

More Than Two Sample Hypothesis Testing Using the ANOVA Table

Source	Sum Squares	df	Mean Square	F Test
Model(Factor)	_____	<u>a - 1</u>	_____	_____
Error	_____	<u>a(n - 1)</u>	_____	
Total	_____	<u>an - 1</u>		

Notes:
a = number of treatments
n = number of items per treatment

Null Hypothesis H_0 : $\mu_1 = \mu_2 = \dots = \mu_a$

Alternate Hypothesis H_1 : At least one treatment is significantly different.

Critical Value: F Distribution Table $F_{0.05, df_{num}, df_{denom}}$

If Reject the Null, conclude at least one treatment is significantly different.

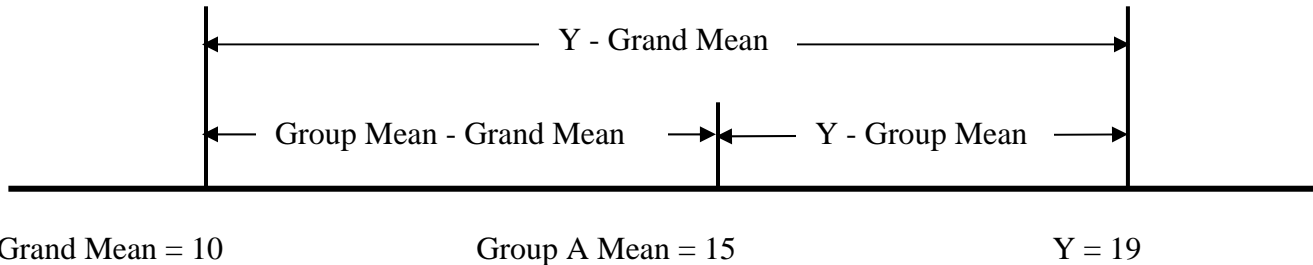
If Fail to Reject, conclude no significant difference between treatments.

ANOVA Model - Sources of Variances

Data Table

Group						Total	Average
A	16	18	10	12	19	75	15
B	4	6	8	10	2	30	6
C	2	10	9	13	11	45	9
					Grand =	150	10

Pick $Y(1,5) = 19$



Deviations

$Y - \text{Grand Mean} = \text{Total Deviations}$

$Y - \text{Group Mean} = \text{Within Group Deviations}$

$\text{Group Mean} - \text{Grand Mean} = \text{Between Groups Deviations}$

Variations

$\text{Sum of Squares Total} = \text{Sum of Squares Between} + \text{Sum Squares Within}$

$\text{Sum of Squares Total} = \text{Sum of Squares Treatment} + \text{Sum Squares Errors}$

$SST = SST_{\text{treat}} + SSE$

$a = \text{Number of Groups}$

$n = \text{Number of Items per Group}$

$an = \text{Total Number of Items}$

Source of Variation	Sum Squares	df	Mean Square
Treatment	SST_{treat}	$a - 1$	$SST_{\text{treat}} / (a - 1)$
Error	SSE	$a(n - 1)$	$SSE / [a(n - 1)]$
Total	SST	$an - 1$	

Note: $(a - 1) + a(n - 1) = a - 1 + an - a = an - 1$

$F_{\text{Test}} = MST_{\text{treat}} / MSE$