

**Homework #3 - Chapter 3 (Montgomery & Runger, 5ed)**

Chapter 3 Discrete Random Variables and Probability Distributions

**Problems:**

Answers to odd-numbered problems can be found in Appendix B.

Answers to even-numbered problems are provided below.

3-4 Mean and Variance of Discrete Random Variable

Page 75, Example 3-10

Page 76, Example 3-11

Page 76, Problems 3-49, 51, 55

3-5 Discrete Uniform Distribution

Page 79, Problems 3-65, 67, 71

3-6 Binomial Distribution

Pages 84, Problems 3-77, 79, 85, 86, 87

3-9 Poisson Distribution

Pages 101 - 103, Problems 3-129, 132, 137, 139, 140

3-86. Let  $X$  denote the number of questions answered correctly. Then,  $X$  is binomial with  $n = 25$  and  $p = 0.25$ .

$$\text{a) } P(X \geq 20) = \binom{25}{20} 0.25^{20} (0.75)^5 + \binom{25}{21} 0.25^{21} (0.75)^4 + \binom{25}{22} 0.25^{22} (0.75)^3 + \binom{25}{23} 0.25^{23} (0.75)^2 + \binom{25}{24} 0.25^{24} (0.75)^1 + \binom{25}{25} 0.25^{25} (0.75)^0 = 9.677 \times 10^{-10}$$

$$\text{b) } P(X < 5) = \binom{25}{0} 0.25^0 (0.75)^{25} + \binom{25}{1} 0.25^1 (0.75)^{24} + \binom{25}{2} 0.25^2 (0.75)^{23} + \binom{25}{3} 0.25^3 (0.75)^{22} + \binom{25}{4} 0.25^4 (0.75)^{21} = 0.2137$$

3-132. Let  $X$  denote the number of calls in one hour. Then,  $X$  is a Poisson random variable with  $\lambda = 10$ .

$$\text{a) } P(X = 5) = \frac{e^{-10} 10^5}{5!} = 0.0378$$

$$\text{b) } P(X \leq 3) = e^{-10} + \frac{e^{-10} 10}{1!} + \frac{e^{-10} 10^2}{2!} + \frac{e^{-10} 10^3}{3!} = 0.0103$$

c) Let  $Y$  denote the number of calls in two hours. Then,  $Y$  is a Poisson random variable with  $\lambda = 20$ .

$$P(Y = 15) = \frac{e^{-20} 20^{15}}{15!} = 0.0516$$

d) Let  $W$  denote the number of calls in 30 minutes. Then  $W$  is a Poisson random variable with  $\lambda = 5$ .

$$P(W = 5) = \frac{e^{-5} 5^5}{5!} = 0.1755$$

3-140. a) Let  $X$  denote the failures in 8 hours. Then,  $X$  has a Poisson distribution with  $\lambda = 0.16$ .

b) Let  $Y$  denote the number of failure in 24 hours. Then,  $Y$  has a Poisson distribution with  $\lambda = 0.48$ .